Mathematics

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Faculty

Associate Professor C. Chindris**, A. Harcharras**, C. Morpurgo**, J. Segert*, D. T. Weston**
Assistant Professor P. Pivovarov**, S. Walsh**, S. Takeda**, J. Tu**
Business Mathematics Coordinator S. Goldschmidt
Calculus Coordinator A. Clayton
College Algebra Coordinator T. E. Christiansen

* Graduate Faculty Member - membership is required to teach graduate-level courses, chair master's thesis committees, and serve on doctoral examination and dissertation committees.
** Doctoral Faculty Member - membership is required to chair doctoral examination or dissertation committees. Graduate faculty membership is a prerequisite for Doctoral faculty membership.

Undergraduate

- Department Level Requirements (http://catalog.missouri.edu/undergraduategraduate/collegeofartsandscience/mathematics/department-level-requirements)
- BA in Mathematics (http://catalog.missouri.edu/undergraduategraduate/collegeofartsandscience/mathematics/ba-mathematics)
- BS in Mathematics (http://catalog.missouri.edu/undergraduategraduate/collegeofartsandscience/mathematics/ba-mathematics)

The Department of Mathematics offers a major with either a Bachelor of Arts or a Bachelor of Science degree. Within the BS degree, an emphasis in Actuarial Science and Financial Mathematics is available. Both the BA and BS degrees will prepare a student for a graduate program in Mathematics.

Preparation for Graduate Study in Mathematics

Students satisfying the requirements for either the BA or the “traditional” BS will have the basic preparation for a graduate program in Mathematics. A student considering graduate work, however, should take additional coursework. Because of this, a BS degree would be considered preferable. Those students in the Actuarial Science area considering graduate work should take MATH 4720 as part of their program. Those students getting a dual degree in Mathematics and Mathematics Education considering graduate work in mathematics should choose to take both MATH 4700 and MATH 4720 as part of their program.

Courses recommended for students planning to pursue graduate studies in pure mathematics: MATH 4400, MATH 4500, MATH 4900, MATH 4920, and MATH 4940.

Courses recommended for students planning to pursue graduate studies in applied mathematics: MATH 4300, MATH 4310, MATH 4315, MATH 4320, MATH 4500, MATH 4540, MATH 4940.

Departmental Honors

Eligibility

To become a candidate for the BA or BS degree with a major in Mathematics with departmental honors, a student must have a cumulative grade point average that meets the Honors College standards. At present, students with a GPA of 3.30 or higher are automatically eligible to enter the departmental honors programs.

Requirements

To graduate with departmental honors in mathematics, a student must satisfy the regular BA or BS degree requirements and must have a GPA of 3.5 or higher in all Mathematics Department courses. In addition, the student must have at least 26 credits in mathematics courses numbered 4000 or above. Furthermore, the student must complete one of the two options listed below.

Option 1: Honors Thesis

The student must write an honors thesis in conjunction with a mentorship or in conjunction with MATH 4996. This option requires that the student enroll in MATH 4996.

Option 2:

The student’s program of study must include MATH 4700, MATH 4900, MATH 4720 and MATH 4920.

Graduate

- MA in Mathematics (http://catalog.missouri.edu/undergraduategraduate/collegeofartsandscience/mathematics/ma-mathematics)
- MS in Applied Mathematics (http://catalog.missouri.edu/undergraduategraduate/collegeofartsandscience/mathematics/ms-applied-mathematics)
- MST in Mathematics (http://catalog.missouri.edu/undergraduategraduate/collegeofartsandscience/mathematics/mst-mathematics)
PhD in Mathematics (http://catalog.missouri.edu/undergraduate/collegeofartsandscience/mathematics/phd-mathematics)

College of Arts and Science
202 Mathematical Sciences Building
(573) 882-6221
https://www.math.missouri.edu/grad/index

Director of Graduate Studies: Stephen Montgomery-Smith

About Mathematics

The Graduate Program in Mathematics is large enough to encompass research and courses in many areas, yet small enough to remain responsive to the needs of individual students. There are approximately 80 graduate students, 40 professors, and 15 postdoctoral and visiting researchers. The active areas of research include: algebraic geometry, analysis (real, complex, functional and harmonic), analytic functions, applied mathematics, financial mathematics and mathematics of insurance, commutative rings, scattering theory, differential equations (ordinary and partial), differential geometry, dynamical systems, general relativity, mathematical physics, number theory, probabilistic analysis and topology.

The Mathematical Sciences Building houses a library with more than 34,000 volumes and 430 journal titles. MU students have access to an extensive array of computing resources.

Admission Notice

Applicants for any graduate degree in mathematics should submit an application for graduate study. Admission to the graduate program does NOT guarantee admission to the Ph.D. program. International Applicants applying from outside North America who seek financial support from the Department will only be considered for the PhD program.

Financial Aid from the Program

All domestic applications for admission are automatically considered for financial support, in most cases by Teaching Assistantships. Virtually all current students are supported financially. Scholarships, assistantships, fellowships and other sources of aid are available.

The Department Research Fellowship, the Blumenthal Scholarship and the McFarlan Fellowship are administered by the department, while the Huggins Scholarship, Gregory Fellowship and Ridgel Fellowship are administered by the university.

International applications with TOEFL of 85 or higher (or equivalent) will also be automatically considered for departmental financial support.

MATH _0110: Intermediate Algebra
MATH _0110 is a preparatory course for college algebra that carries no credit towards any baccalaureate degree. However, the grade received in MATH _0110 does count towards a student's overall GPA. The course covers operations with real numbers, graphs of functions, domain and range of functions, linear equations and inequalities, quadratic equations; operations with polynomials, rational expressions, exponents and radicals; equations of lines. Emphasis is also put on problem-solving.

Credit Hours: 3

MATH 1050: Quantitative Reasoning
Promotes mathematical literacy among students. This course will cover important mathematical ideas and problem solving skills in the context of science, technology, and/or society. Topics may include: logic and critical thinking, Venn Diagrams, problem solving, sets, units of measure, percentages and ratios, counting and probability, exponential growth and decay, linear and exponential models. Quantitative Reasoning is designed to stimulate interest in and appreciation of mathematics and quantitative reasoning as valuable tools for comprehending the world in which we live. This course does not satisfy the prerequisite of any other MATH course.

Credit Hours: 3
Prerequisites: C- or higher in MATH _0110 or a sufficient score on the myMath test

MATH 1100 - MOTR MATH 120: Mathematical Reasoning Modeling

MATH 1110: College Algebra
A review of exponents, order of operations, factoring, and simplifying polynomial, rational, and radical expressions. Topics include: linear, quadratic, polynomial, rational, inverse, exponential, and logarithmic functions and their applications. Students will solve equations involving these functions, and systems of linear equations in two variables, as well as inequalities. See the Math website for specific requirements. A student may receive at most 5.0 credit hours among MATH 1100, MATH 1120, MATH 1140, MATH 1160.

Credit Hours: 3
Prerequisites: C- or higher in MATH _0110 or a sufficient score on the ALEKS exam or MyMathTest Intermediate Algebra score of 70% or higher

MATH 1110 - MOTR MATH 130: Pre-Calculus Algebra

MATH 1140: Trigonometry
A student may receive only 5 credits from among MATH 1100, MATH 1140, and MATH 1160. A student may receive at most 5.0 credit hours from MATH 1100, MATH 1120, MATH 1140, and MATH 1160.

Credit Hours: 2
Prerequisites: C- or higher in MATH 1100 or sufficient ALEKS score or MyMathTest College Algebra score of 70% or higher

MATH 1160: Precalculus Mathematics
Review of elementary algebra. Background material for MATH 1500, including algebraic, trigonometric, logarithmic, exponential functions. A student may receive at most 5 credits from among MATH 1100, MATH 1140, and MATH 1160.

Credit Hours: 5
Prerequisites: B+ or higher in MATH _0110 (at MU), or C- or higher in MATH 1100, or sufficient ALEKS score or MyMathTest College Algebra score of 60% or higher

MATH 1160 - MOTR MATH 150: Pre-Calculus

MATH 1300: Finite Mathematics
A selections of topics in finite mathematics such as: basic financial mathematics, counting methods and basic probability and statistics, systems of linear equations and matrices. Warning: without a College Algebra exemption, a sufficient ALEKS score will not suffice unless it is a proctored exam (for MATH 1100 credit).
MATH 1360: Geometric Concepts
This course is primarily for education majors. This course covers topics of Euclidean geometry such as the study of points, lines, angles, polygons, circles, congruence, similarity, transformations, symmetry, area, surface area, arc length, and volume. Polyhedra, spheres, cones, and other solids are discussed. The course includes constructions and proofs, and uses inductive and deductive reasoning throughout. Math Reasoning Proficiency Course.

Credit Hours: 3
Prerequisites: Grade of C- or higher in MATH 1100, or MATH 1160, or both a College Algebra exemption and sufficient ALEKS score

MATH 1400: Calculus for Social and Life Sciences I
The real number system, functions, analytic geometry, derivatives, integrals, maximum-minimum problems. No credit for students who have completed a calculus course. A student may receive credit for MATH 1320 or MATH 1400 but not both. A student may receive at most 5 units of credit among the MATH 1320 or MATH 1400 and MATH 1500. Math Reasoning Proficiency Course.

Credit Hours: 3
Prerequisites: C- or higher in MATH 1100 or sufficient ALEKS exam score or MATH 1160 or equivalent

MATH 1500: Analytic Geometry and Calculus I
Elementary analytic geometry, functions, limits, continuity, derivatives, antiderivatives, definite integrals. A student may receive at most 5 units of credit among the Mathematics courses MATH 1320 or MATH 1400 and MATH 1500. Math Reasoning Proficiency Course.

Credit Hours: 5
Prerequisites: grade of C- or higher in MATH 1100 or MATH 1160, or sufficient ALEKS score

MATH 1500H: Analytic Geometry and Calculus I - Honors
Elementary analytic geometry, functions, limits, continuity, derivatives, antiderivatives, definite integrals. Honors eligibility required. A student may receive at most 5 units of credit among MATH 1320 or MATH 1400 and MATH 1500. Math Reasoning Proficiency course.

Credit Hours: 5
Prerequisites: C- or higher in MATH 1160 or C - or higher in both MATH 1100 and MATH 1140 or sufficient ALEKS score or MyMathTest PreCalculus score of 70% or higher

MATH 1601: Selected Topics in Mathematics-General
The special topics covered may vary from term to term. This course may be repeated.

Credit Hour: 1-3
Prerequisites: instructor's consent

MATH 1602: Selected Topics in Mathematics-Biological/Physical/ Math
The special topics covered may vary from term to term. This course may be repeated.

MATH 1700: Calculus II
Definite integrals, applications and techniques of integration, elementary transcendental functions, infinite series. Math Proficiency Reasoning course.

Credit Hours: 5
Prerequisites: a grade of C- or better in MATH 1500

MATH 1700H: Calculus II - Honors
Definite integrals, applications and techniques of integration, elementary transcendental functions, infinite series. Math Reasoning Proficiency course.

Credit Hours: 5
Prerequisites: a grade of C- or better in MATH 1500. Honors eligibility required

MATH 2100: Calculus for Social and Life Sciences II
Riemann integral, transcendental functions, techniques of integration, improper integrals and functions of several variables. No credit for students who have completed two calculus courses. Math Reasoning Proficiency course.

Credit Hours: 3
Prerequisites: C- or higher in MATH 1320 or MATH 1400 or MATH 1500

MATH 2300: Calculus III
Vectors, solid analytic geometry, calculus of several variables. Math Reasoning Proficiency course.

Credit Hours: 3
Prerequisites: grade of C - or better in MATH 1700

MATH 2300H: Calculus III - Honors
Vectors, solid analytic geometry, calculus of several variables. Math Reasoning Proficiency course.

Credit Hours: 3
Prerequisites: grade of C or better in MATH 1700. Honors eligibility required

MATH 2320: Discrete Mathematical Structures
Sets, functions, logic, relations, induction, recursion, counting techniques, graphs, trees, algorithms. Math Reasoning Proficiency course.

Credit Hours: 3
Prerequisites: Grade of C- or higher in MATH 1700

MATH 3000: Introduction to Advanced Mathematics
Gateway to theoretical math courses. Focus on reading and writing math proofs/hugorously developing background needed in Adv Calc/Abstract Alg. Topics include logic, set theory, properties of functions and integers, the real number system, completeness of the real numbers, sequences of real numbers.

Credit Hours: 3
Prerequisites: Consent of Department required. Recommended MATH 1700
MATH 3000W: Introduction to Advanced Mathematics - Writing Intensive
Gateway to theoretical math courses. Focus on reading and writing math proofs/rigorously developing background needed in Adv Calc/Abstract Alg. Topics include logic, set theory, properties of functions and integers, the real number system, completeness of the real numbers, sequences of real numbers.
Credit Hours: 3
Prerequisites: Consent of Department required. Recommended MATH 1700

MATH 4002: Topics in Mathematics-Biological Sciences
Organized study of selected topics. Subjects and earnable credit may vary from semester to semester. May repeat for credit with Departmental consent.
Credit Hour: 1-6
Prerequisites: MATH 2300 and instructor's consent

MATH 4006: Topics in Mathematics-Mathematical Sciences
Organized study of selected topics. Subjects and earnable credit may vary from semester to semester. May repeat for credit with Departmental consent.
Credit Hour: 1-6
Prerequisites: MATH 2300 and instructor's consent

MATH 4007: Topics in Mathematics-Physical Sciences
Organized study of selected topics. Subjects and earnable credit may vary from semester to semester. May repeat for credit with Departmental consent.
Credit Hour: 1-6
Prerequisites: MATH 2300 and instructor's consent

MATH 4060: Connecting Geometry to Middle and Secondary Schools
(cross-leveled with MATH 7060). Euclidean foundations, logic, Euler Characteristic, congruence, area, Pick's Theorem, volume, Cavalieri's Principle, surface area, similarity, symmetry, transformations, matrices, introduction to spherical geometry.
Credit Hours: 3
Prerequisites: Consent of Department required
Recommended: MATH 1360 or MATH 1500

MATH 4070: Connecting Algebra to Middle and Secondary Schools
A detailed study of integer and rational arithmetic and algebra. Topics include: Binomial Theorem, induction, division algorithm, Euclid's Algorithm, Fundamental Theorem of Arithmetic, Pythagorian triples, modular arithmetic and generalizations to polynomials, matrices and other axiomatic structures.
Credit Hours: 3
Prerequisites: MATH 1320, enrollment is restricted to Math Education majors

MATH 4080: Calculus Connections
Course topics include: sequences, series, functions, limits, continuity, differentiation, optimization, curve sketching, antidifferentiation, areas of plane regions, lengths of plane curves, areas of surfaces of revolution, and volumes of solids.
Credit Hours: 3
Prerequisites: MATH 1160, enrollment is restricted to Math Education majors

MATH 4100: Differential Equations
(cross-leveled with MATH 7100). Traditional introductory course in ordinary differential equations. Includes 1st and 2nd order linear differential equations with numerous applications; Laplace transforms; power series solutions; numerical methods, linear systems.
Credit Hours: 3
Prerequisites: Grade of C- or above in MATH 2300

MATH 4140: Matrix Theory
(cross-leveled with MATH 7140). Basic properties of matrices, determinants, vector spaces, linear transformations, eigenvalues, eigenvectors, and Jordan normal forms. Introduction to writing proofs.
Credit Hours: 3
Prerequisites: Grade of C- or better in MATH 2300 or MATH 2320.
Writing intensive sections require ENGLSH 1000

MATH 4140W: Matrix Theory - Writing Intensive
Basic properties of matrices, determinants, vector spaces, linear transformations, eigenvalues, eigenvectors, and Jordan normal forms. Introduction to writing proofs.
Credit Hours: 3
Prerequisites: Grade of C- or better in MATH 2300 or MATH 2320.
Writing intensive sections require ENGLSH 1000

MATH 4150: History of Mathematics
This is a history course with mathematics as its subject. Includes topics in the history of mathematics from early civilizations onwards. The growth of mathematics, both as an abstract discipline and as a subject which interacts with others and with practical concerns, is explored.
Prerequisites or Cirequisite: MATH 2300 or MATH 2340. Writing intensive sections require ENGLSH 1000.
Credit Hours: 3

MATH 4150W: History of Mathematics - Writing Intensive
This is a history course with mathematics as its subject. Includes topics in the history of mathematics from early civilizations onwards. The growth of mathematics, both as an abstract discipline and as a subject which interacts with others and with practical concerns, is explored.
Prerequisites or Cirequisite: MATH 2300 or MATH 2340. Writing intensive sections require ENGLSH 1000.
Credit Hours: 3

MATH 4300: Numerical Analysis
Machine arithmetic, approximation and interpolation, numerical differentiation and integration, nonlinear equations, linear systems,
differential equations, error analysis. Selected algorithms will be programmed for solution on computers.

**Credit Hours:** 3  
**Prerequisites:** Grade of C- or better in MATH 2300 and MATH 4100

### MATH 4310: Numerical Linear Algebra
Solution of linear systems of equations by direct and iterative methods. Calculation of eigenvalues and eigenvectors of matrices. Selected algorithms programmed for solution on computers.

**Credit Hours:** 3  
**Prerequisites:** MATH 2300 and familiarity with software such as Mathematica, MatLab, Maple, etc

### MATH 4315: Introduction to Mathematical Statistics
(same as STAT 4710). Introduction to theory of probability and statistics using concepts and methods of calculus.

**Credit Hours:** 3  
**Prerequisites:** MATH 2300 or instructor's consent

### MATH 4320: Introduction to Probability Theory
(same as STAT 4750). Probability spaces; random variables and their distributions; repeated trials; probability limit theorems.

**Credit Hours:** 3  
**Prerequisites:** MATH 2300 or instructor's consent

### MATH 4330: Theory of Numbers
Divisibility, factorization, arithmetic functions, means value theorems, distribution of prime numbers, congruences, primitive roots, character theory, Riemann zeta function, and Dirichlet L-functions.

**Credit Hours:** 3  
**Prerequisites:** Grade of C- or higher in MATH 2300. Recommended MATH 2320

### MATH 4340: Introduction to Topology
Topics from topology of Euclidean spaces, generalizations to metric spaces and topological spaces. Fundamentals of point set topology.

**Credit Hours:** 3  
**Prerequisites:** MATH 2300

### MATH 4350: Introduction to Non-Euclidean Geometry

**Credit Hours:** 3  
**Prerequisites:** MATH 2300

### MATH 4355: Mathematics of Financial Derivatives I
(cross-leveled with MATH 7355). Long and short positions, forward contracts, exchange traded index futures, European and American call and put options, put-call parity, trading and hedging strategies, synthetic transactions, arbitrage, currency options, fixed income portfolio management, duration, convexity, interest rate and currency swaps, embedded options.

**Credit Hours:** 3  
**Prerequisites:** Grade of C- or higher in MATH 2300 and either STAT 2500 or STAT 4710 or MATH 4315

### MATH 4370: Interest Theory
(cross-leveled with MATH 7370). This course covers the concepts underlining the theory of interest and their applications to valuation of various cash flows, annuities certain, bonds, and loan repayment. This course is designed to help students prepare for Society of Actuaries exam FM (Financial Mathematics). It is oriented towards problem solving techniques applied to real-life situations and illustrated with previous exam problems.

**Credit Hours:** 3  
**Prerequisites:** grade of C- or better in MATH 2300

### MATH 4371: Models for Life Contingencies I
(cross-leveled with MATH 7371). The sequence MATH 4371 - MATH 4372 is designed to help students prepare for the Society of Actuaries exam LTAM (Long-Term Actuarial Mathematics). This course teaches the basic theory of life contingent actuarial models and the applications of those models to insurance and other financial risks. Covered topics include: survival models, life tables and selection, insurance benefits, life annuities, premium calculation and reserves.

**Credit Hours:** 3  
**Prerequisites:** MATH 4320 or STAT 4750, and MATH 4370

### MATH 4372: Models for Life Contingencies II
(cross-leveled with MATH 7372). The sequence MATH 4371 - MATH 4372 is designed to help students prepare for the Society of Actuaries exam LTAM (Long-Term Actuarial Mathematics). This course extends the life-death contingency models of Math 4371 to more general multiple-state and multiple-life models applied to problems involving a wide range of insurance and pension benefits. Covered topics include: Markov chains, multiple decrement models, joint life and last survivor benefits, pension mathematics, profit testing.

**Credit Hours:** 3  
**Prerequisites:** A grade of C- or better in MATH 4371

### MATH 4400: Introduction to Topology
Topics from topology of Euclidean spaces, generalizations to metric spaces and topological spaces. Fundamentals of point set topology.

**Credit Hours:** 3  
**Prerequisites:** MATH 2300

### MATH 4450: Applied Analysis
Solution of the standard partial differential equations (wave, heat, Laplace's eq.) by separation of variables and transform methods; including eigenfunction expansions, Fourier and Laplace transform. Boundary value problems, Sturm-Liouville theory, orthogonality, Fourier, Bessel, and Legendre series, spherical harmonics.

**Credit Hours:** 3  
**Prerequisites:** Grade of C- or higher in MATH 4100

### MATH 4510: Higher Algebra
Introduction to rings, integral domains, fields, groups.

**Credit Hours:** 3  
**Prerequisites:** Grade of C- or higher in MATH 2300 or MATH 2320

### MATH 4520: Statistical Inference I
(same as STAT 4760). Sampling; point estimation; sampling distribution; tests of hypotheses; regression and linear hypotheses.

**Credit Hours:** 3  
**Prerequisites:** MATH 4320
MATH 4540: Mathematical Modeling I
Solution of problems from industry, physical, social and life sciences, economics, and engineering using mathematical models.
Credit Hours: 3
Prerequisites: Grade of C- or higher in MATH 2300 and MATH 4100
Recommended: Familiarity with software such as MATHEMATICA, MATLAB, or MAPLE

MATH 4560: Nonlinear Dynamics, Fractals and Chaos
Conceptual introduction to nonlinear dynamics, bifurcation and stability of steady states, chaos in nonlinear differential equations and maps, fractal dimension, strange attractors, and applications to physical science.
Credit Hours: 3
Prerequisites: MATH 4100 or MATH 7100, MATH 4140 or MATH 7140, and familiarity with software such as MATHEMATICA, MATLAB, or MAPLE

MATH 4590: Mathematics of Financial Derivatives II
Credit Hours: 3
Prerequisites: MATH 2300 and either STAT 2500 or STAT 4710 or MATH 4315
Recommended: MATH 4355

MATH 4700: Advanced Calculus of One Real Variable I
(cross-leveled with MATH 7700). Basic topology of the real line, numerical sequences and series, continuity, differentiability, Riemann integration, uniform convergence, power series.
Credit Hours: 3
Prerequisites: Grade of C- or higher in MATH 3000

MATH 4720: Introduction to Abstract Algebra I
Basic properties of integers, fundamental theorem of arithmetic, introduction to groups, rings and fields.
Credit Hours: 3
Prerequisites: Grade of C- or higher in MATH 3000

MATH 4740: Advanced Multivariable Calculus
(cross-leveled with MATH 7900). This is a course in calculus in several variables. The following is core material: Basic topology of n-dimensional Euclidan space; limits and continuity of functions; the derivative as a linear transformation; Taylor's formula with remainder; the Inverse and Implicit Function Theorems; change of coordinates; integration (including transformation of integrals under changes of coordinates); Green's Theorem. Additional material from the calculus of several variables may be included, such as Lagrange multipliers, differential forms, etc.
Credit Hours: 3
Prerequisites: MATH 4700

MATH 4920: Introduction to Abstract Linear Algebra
(cross-leveled with MATH 7920). Study of vector spaces over arbitrary fields: topics include linear maps on finite dimensional vector spaces, bilinear and multi-linear forms, invariant subspaces and canonical forms.
Credit Hours: 3
Prerequisites: Grade of C- or higher in MATH 4720

MATH 4940: Introduction to Complex Variables
Complex functions, contour integration, power series, residues and poles, conformal mapping.
Credit Hours: 3
Prerequisites: MATH 4110 or MATH 4700

MATH 4960: Special Readings in Mathematics
Credit Hour: 1-3
Prerequisites: Consent of Department required

MATH 4996: Honors in Mathematics
Special work for senior B.A. Honors and B.S. Honors candidates.
Credit Hours: 2
Prerequisites: Consent of Department required

MATH 7100: Differential Equations
(cross-leveled with MATH 4100). Traditional introductory course in ordinary differential equations. Includes 1st and 2nd order linear differential equations with numerous applications; Laplace transforms; power series solutions; numerical methods, linear systems.
Credit Hours: 3
Prerequisites: graduate standing and MATH 2300

MATH 7140: Matrix Theory
(cross-leveled with MATH 4140). Basic properties of matrices, determinants, vector spaces, linear transformations, eigenvalues, eigenvectors, and Jordan normal forms. Introduction to writing proofs.
Credit Hours: 3
Prerequisites: graduate standing and one of MATH 2300, MATH 2320, MATH 2120 or MATH 2340

MATH 7150: History of Mathematics
This is a history course with mathematics as its subject. Includes topics in the history of mathematics from early civilizations onwards. The growth of mathematics, both as an abstract discipline and as a subject which interacts with others and with practical concerns, is explored. Pre- or Co-requisite: MATH 2300 or MATH 2340 and graduate standing.
Credit Hours: 3

MATH 7300: Numerical Analysis
Machine arithmetic, approximation and interpolation, numerical differentiation and integration, nonlinear equations, line ar systems, differential equations, error analysis. Selected algorithms will be programmed for solution on computers.
Credit Hours: 3
Prerequisites: graduate standing and MATH 2300 and MATH 4100 or equivalent
**Mathematics**

**MATH 7310: Numerical Linear Algebra**
Solution of linear systems of equations by direct and iterative methods. Calculation of eigenvalues and eigenvectors of matrices. Selected algorithms programmed for solution on computers.

**Credit Hours: 3**

**Prerequisites:** MATH 2300 and prior experience writing programs in Mathematica and/or in a computer language such as Fortran, Pascal, or C.

**Recommended:** MATH 4140

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**MATH 7330: Theory of Numbers**
Divisibility, factorization, arithmetic functions, means value theorems, distribution of prime numbers, congruences, primitive roots, character theory, Riemann zeta function, and Dirichlet L-functions.

**Credit Hours: 3**

**Prerequisites:** MATH 2300; recommended MATH 2320 or MATH 2340, and MATH 4940 or MATH 7940

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**MATH 7355: Mathematics of Financial Derivatives I**
(cross-leveled with MATH 4355). Long and short positions, forward contracts, exchange traded index futures, European and American call and put options, put-call parity, trading and hedging strategies, synthetic transactions, arbitrage, currency options, fixed income portfolio management, duration, convexity, interest rate and currency swaps, embedded options.

**Credit Hours: 3**

**Prerequisites:** MATH 2300 and STAT 2500 or STAT 4710/ MATH 4315, or instructor's consent

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**MATH 7370: Interest Theory**
(cross-leveled with MATH 4370). This course covers the main probability tools applied to financial risk modeling, and the financial mathematics concepts used in calculating present and accumulated values for various cash flows. It is a helpful tool in preparing for the Society of Actuaries exams P (Probability) and FM (Financial Mathematics), and it is oriented towards problem solving techniques illustrated with previous exam problems. Students are encouraged to take MATH 4355 prior to this course.

**Credit Hours: 3**

**Prerequisites:** MATH 2300, MATH 4320/ STAT 4750

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**MATH 7371: Models for Life Contingencies I**
(cross-leveled with MATH 4371). The sequence MATH 4371 - MATH 4372 is designed to help students prepare for the Society of Actuaries exam LTAM (Long-Term Actuarial Mathematics). This course teaches the basic theory of life contingent actuarial models and the applications of those models to insurance and other financial risks. Covered topics include: survival models, life tables and selection, insurance benefits, life annuities, premium calculation and reserves.

**Credit Hours: 3**

**Prerequisites:** MATH 2300, MATH 4320/ STAT 4750

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**MATH 7372: Models for Life Contingencies II**
(cross-leveled with MATH 4372). The sequence MATH 4371 - MATH 4372 is designed to help students prepare for the Society of Actuaries exam LTAM (Long-Term Actuarial Mathematics). This course extends the life-death contingency models of MATH 4371 to more general multiple-state and multiple-life models applied to problems involving a wide range of insurance and pension benefits. Covered topics include: Markov chains, multiple decrement models, joint life and last survivor benefits, pension mathematics, profit testing.

**Credit Hours: 3**

**Prerequisites:** A grade of C- or better in MATH 4371 or MATH 7371

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**MATH 7400: Introduction to Topology**
Topics from topology of Euclidean spaces, generalizations to metric spaces and topological spaces. Fundamentals of point set topology.

**Credit Hours: 3**

**Prerequisites:** MATH 2300

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**MATH 7500: Applied Analysis**
Solution of the standard partial differential equations (wave, heat, Laplace's eq.) by separation of variables and transform methods; including eigenfunction expansions, Fourier and Laplace transform. Boundary value problems, Sturm-Liouville theory, orthogonality, Fourier, Bessel, and Legendre series, spherical harmonics.

**Credit Hours: 3**

**Prerequisites:** MATH 4100/ MATH 7100

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**MATH 7510: Higher Algebra**
Introduction to rings, integral domains, fields, groups.

**Credit Hours: 3**

**Prerequisites:** MATH 2300 OR MATH 2320

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**MATH 7540: Mathematical Modeling I**
Solution of problems from industry, physical, social and life sciences, economics, and engineering using mathematical models.

**Credit Hours: 3**

**Prerequisites:** graduate standing and 3 semesters of calculus and some exposure to ordinary differential equations or instructor's consent

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**MATH 7560: Nonlinear Dynamics, Chaos and Fractals**
Conceptual introduction to nonlinear dynamics, bifurcation and stability of steady states, chaos in nonlinear differential equations and maps, fractal dimension, strange attractors, and applications to physical science.

**Credit Hours: 3**

**Prerequisites:** graduate standing and MATH 4100/ MATH 7100, MATH 4140/ MATH 7140, and familiarity with software such as MATHEMATICA, MATLAB, or MAPLE

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**MATH 7590: Mathematics of Financial Derivatives II**
(cross-leveled with MATH 4590). Binomial and Black-Scholes pricing models. Option Greeks, delta and gamma hedging, market maker profit theory. Asian, barrier, compound, gap and exchange options. Lognormal and Monte Carlo price simulation. Geometric Brownian Motion and Ito's Lemma. Interest rate models and volatility. Prerequisites: MATH 2300 and either STAT 2500 or STAT 4710 or MATH 4315.

**Credit Hours: 3**

**Prerequisites:** MATH 2300 and either STAT 2500 or STAT 4710 or MATH 4315

**Recommended:** MATH 4355
MATH 7700: Advanced Calculus of One Real Variable I
(cross-leveled with MATH 4700). Series of real numbers, limits of functions, continuity and uniform continuity, differentiability, and Riemann integration.

Credit Hours: 3
Prerequisites: MATH 2300
Recommended: MATH 4140 and one other mathematics course number above MATH 2300

MATH 7720: Introduction to Abstract Algebra I
Basic properties of integers, fundamental theorem of arithmetic, introduction to groups, rings and fields.

Credit Hours: 3
Prerequisites: MATH 2300
Recommended: MATH 4140 and one other Mathematics course numbered above 2300

MATH 7900: Advanced Multivariable Calculus
(cross-leveled with MATH 4900). This is a course in calculus in several variables. The following is core material: Basic topology of n-dimensional Euclidian space; limits and continuity of functions; the derivative as a linear transformation; Taylor's formula with remainder; the Inverse and Implicit Function Theorems, change of coordinates; integration (including transformation of integrals under changes of coordinates); Green's Theorem. Additional material from the calculus of several variables may be included, such as Lagrange multipliers, differential forms, etc.

Credit Hours: 3
Prerequisites: MATH 4700/ MATH 7700

MATH 7920: Introduction to Abstract Linear Algebra
Study of vector spaces over arbitrary fields: topics include linear maps on finite dimensional vector spaces, bilinear and multi-linear forms, invariant subspaces and canonical forms.

Credit Hours: 3
Prerequisites: MATH 2300

MATH 7940: Introduction to Complex Variables
Complex functions, contour integration, power series, residues and poles, conformal mapping.

Credit Hours: 3
Prerequisites: MATH 4110/ MATH 7110 OR MATH 4700/ MATH 7700

MATH 7960: Special Readings in Mathematics
Credit Hour: 1-3
Prerequisites: MATH 2300 and instructor's consent

MATH 7980: Mathematics Problem Solving
Creative advanced problem solving bringing together methods such as integration, probability and Euclidean geometry.

Credit Hours: 3
Prerequisites: MATH 4140 and another 4000 level Mathematics course, or instructor's consent

MATH 8085: Problems in Mathematics
Problems in Mathematics

Credit Hours: 3

MATH 8090: Master's Thesis Research in Mathematics
Students will be required to complete an independent project. Topics are chosen in consultation with a faculty advisor and are subject to departmental consent. Graded on S/U basis only.

Credit Hours: 3

MATH 8102: Topics in Algebra
Advanced topics in algebra.

Credit Hours: 3
Prerequisites: MATH 8410

MATH 8190: Masters Project in Mathematics
Masters Project in Mathematics

Credit Hours: 3

MATH 8202: Topics in Functional Analysis
Topics in Functional Analysis

Credit Hours: 3

MATH 8210: Basic Algebra
Accelerated problem solving course in linear and abstract algebra. Will prepare students for the algebra qualifying exam.

Credit Hours: 3
Prerequisites: MATH 4720, MATH 4920, or instructor's consent, or equivalent
Corequisites: MATH 8220 and MATH 8250

MATH 8220: Basic Analysis
Accelerated problem-solving course in advanced calculus and complex analysis. Will prepare students for the analysis qualifying exam.

Credit Hours: 6
Prerequisites: MATH 4700, MATH 4900, MATH 4940, instructor's consent or equivalent

MATH 8250: Basic Topology and Geometry

Credit Hours: 3
Prerequisites: MATH 4700, MATH 4900, MATH 4140, or instructor's consent, or equivalent
Corequisites: MATH 8210 and MATH 8220

MATH 8302: Topics in Harmonic Analysis
Topics in Harmonic Analysis

Credit Hours: 3

MATH 8402: Topics in Mathematical Physics
Topics in Mathematical Physics
Credit Hours: 3

MATH 8410: Algebra I
Theory of algebraic structures—groups, rings, fields, algebraic and transcendental extensions of fields.
Credit Hours: 3
Prerequisites: MATH 4720 and MATH 4920, or equivalent

MATH 8411: Algebra II
Theory of modules, Galois theory and additional topics to be selected by the instructor.
Credit Hours: 3
Prerequisites: MATH 8410 or equivalent

MATH 8420: Theory of Functions of Real Variables I
Properties of functions of one real variable. Lebesgue measure and integration on the line.
Credit Hours: 3
Prerequisites: MATH 4700 or MATH 7700 and MATH 4900 or MATH 7900, or equivalent

MATH 8421: Theory of Functions of Real Variables II
Continuation of MATH 8420. General measure and integration theory. Elements of the theory of Hilbert and Banach spaces, linear functions and linear operators.
Credit Hours: 3
Prerequisites: MATH 8420

MATH 8425: Complex Analysis I
Rigorous introduction to the theory of functions of a complex variable.
Credit Hours: 3
Prerequisites: MATH 4940 or MATH 7940 or equivalent

MATH 8426: Complex Analysis II
Analytic continuation, Riemann surfaces, entire and meromorphic functions, selected topics.
Credit Hours: 3
Prerequisites: MATH 4940 or MATH 7940 or equivalent

MATH 8440: Advanced Ordinary Differential Equations I
Topics from existence and uniqueness theorems, plane autonomous systems, periodicity and boundedness of solutions of second order nonlinear equations, perturbation theory, Sturm-Liouville systems, behavior of solutions at singularities.
Credit Hours: 3
Prerequisites: MATH 4700 or MATH 7700 or equivalent

MATH 8445: Partial Differential Equations I
Fourier and integral transforms, first and second order partial differential equations, methods of characteristics, Laplace's equation, Dirichlet and Neumann problems, Green's functions and maximum principles.
Credit Hours: 3
Prerequisites: MATH 4700 or MATH 7700 or instructor's consent required

MATH 8446: Partial Differential Equations II
The Cauchy-Kovalevski theorem, the Lewy example, the heat operator, the wave operator, Sobolev spaces, local regularity of elliptic boundary value problems.
Credit Hours: 3
Prerequisites: MATH 8445
Recommended: MATH 8420

MATH 8460: Mathematical Finance I
Credit Hours: 3
Prerequisites: graduate standing in Mathematics. Knowledge of elementary probability or instructor's consent

MATH 8461: Mathematical Finance II
Credit Hours: 3
Prerequisites: knowledge of advance probability/stochastic processes or instructor's consent
Recommended: MATH 8460

MATH 8480: Advanced Probability
(same as STAT 9810). Measure theoretic probability theory. Characteristic functions; conditional probability and expectation; sums of independent random variables including strong law of large numbers and central limit problem.
Credit Hours: 3
Prerequisites: MATH 4320 or MATH 8220; or instructor's consent

MATH 8502: Topics of Geometry
Topics of Geometry.
Credit Hours: 3
Prerequisites: instructor's consent

MATH 8587: Topology Seminar
Topology Seminar
Credit Hours: 3

MATH 8615: Algebraic Geometry I
Affine and projective varieties and schemes; nullstellensatz; Zariski topology, morphisms and rational maps; divisors and linear systems;
topics from curves, surfaces, Grassmann varieties; commutative algebra and homological algebra as needed.

Credit Hours: 3
Prerequisites: MATH 8410

MATH 8616: Algebraic Geometry II
Continuation of MATH 8615.
Credit Hours: 3
Prerequisites: MATH 8615

MATH 8618: Introduction to Algebraic Topology
Development of singular homology theory; reference to other homology and cohomology theories. Introduction to homological algebra.
Credit Hours: 3
Prerequisites: MATH 8250

MATH 8628: Functional Analysis I
Linear topological spaces, Banach spaces, Hilbert spaces. Operator theory, including the Hahn-Banach, uniform boundedness and closed graph theorems.
Credit Hours: 3
Prerequisites: MATH 4900 and instructor's consent or MATH 8420

MATH 8630: Harmonic Analysis I
An introduction to Fourier Analysis in one and higher Dimensions. Topics include Fourier Series, conjugate functions, Fourier transforms, distributions, interpolation, and maximal functions.
Credit Hours: 3
Prerequisites: MATH 8420

MATH 8631: Harmonic Analysis II
Singular integrals, Littlewood-Paley theory, Hardy spaces, bounded mean oscillation, weighted norm inequalities, boundary value problems, and analysis on groups.
Credit Hours: 3
Prerequisites: MATH 8630

MATH 8650: Differentiable Manifolds and Riemannian Geometry
Tensor product spaces and tensor fields on manifolds. Differentiation and integration of differential forms. Riemannian geometry and applications.
Credit Hours: 3
Prerequisites: MATH 4700 or MATH 4400

MATH 8655: General Topology I
Credit Hours: 3
Prerequisites: MATH 4900, MATH 4400 or instructor's consent

MATH 8702: Topics in Applied Mathematics
Selected topics in applied mathematics drawn from variety of areas: partial differential equations, tensor analysis, calculus of variations, asymptotic methods, integral equations, advanced theory of transforms and distributions, numerical analysis.
Credit Hours: 3

MATH 9090: Doctoral Dissertation Research in Mathematics
Doctoral Dissertation Research in Mathematics. Graded on a S/U basis only.
Credit Hour: 1-9

MATH 9387: Harmonic Analysis Seminar
Harmonic Analysis Seminar
Credit Hours: 3

MATH 9487: Mathematical Physics Seminar
Mathematical Physics Seminar
Credit Hours: 3

MATH 9502: Topics in Topology
Advanced topics in topology or topological algebra.
Credit Hours: 3

MATH 9787: Applied Mathematics Seminar
Applied Mathematics Seminar
Credit Hours: 3

MATH 9887: Analysis Seminar
Analysis Seminar
Credit Hours: 3